

*A Study of Extra Special p-group*

**DISSERTATION**

**SUBMITTED IN PARTIAL FULFILMENT OF THE REQUIREMENT FOR  
THE AWARD OF DEGREE OF**

**MASTER OF SCIENCE IN MATHEMATICS**

*BY*

**Murtadha Ali Shabeeb**

**(ID.NO.11MSMATH006)**

**Advisor: Dr. Swapnil Srivastava**



**2012-2013**

**DEPARTMENT OF MATHEMATICS & STATISTICS**

**SCHOOL OF BASIC SCIENCES**

**SAM HIGGINBOTTOM INSTITUTE OF AGRICULTURE, TECHNOLOGY  
& SCIENCES**

**ALLAHABAD -211007(U.P)**

**2013**

## ABSTRACT

In this dissertation we have discussed extra special  $p$ -group. A finite non-abelian  $p$ -group is called extra special  $p$ -group if its center is exactly equal to its commutator subgroup. Here we have discussed extra special  $p$ -groups and we have find that every non-abelian group of order  $p^3$  is extra special  $p$ -group. In particular if  $p = 2$  then we have two extra special  $p$ -groups one is dihedral group  $D_4$  and another is Hamiltonian group  $Q_8$ .

Here we have also discussed that if  $G$  is non-abelian group of order  $p^3$ , then  $Z(G)$  has order  $p$ . We have thoroughly discussed the following theorem:

Let  $G$  be a finite extra special group. Then it is central product of non-abelian groups of order  $p^3$ . In particular  $G$  is of order  $p^{2m+1}$  for some  $m$ .

To prove above theorem we have gone through solvability and nilpotency in groups, Frattini subgroups, and different type of bilinear forms.

## Conclusion

- ✓ We have solved extra Special  $p$ -group of order  $p^3$ , where  $p$  is even prime discussed, we have find that one is  $Q_8$  and second is  $D_4$  .
- ✓ We have proved that every non-abelian group of order  $p^3$  is extra special  $p$ -group.
- ✓ We have proved that  $G$  be a finite extra special group, then it is central product of non-abelian groups of order  $p^3$ . In particular  $G$  is of order  $p^{2m+1}$  for some  $m$ .